

Palindromes (simplified)

grammar Palindrome

nonterminal P(2), S(0);
terminal a(2), b(2);
start S;

S() ::= P(x,y) [init]
P(x,y) ::= a(x,u) a(v,y) P(u,v) [aPa]
 | b(x,u) b(v,y) P(u,v) [bPb]
 | a(x,u) a(u,y) [aa]
 | b(x,u) b(u,y) [bb]

end

State $q_0(a, b)$

S()	→ .P(a, b)
P(a, b)	→ .a(a, n ₁) a(n ₁ , b)
P(a, b)	→ .a(a, n ₂) a(n ₃ , b) P(n ₂ , n ₃)
P(a, b)	→ .b(a, n ₄) b(n ₄ , b)
P(a, b)	→ .b(a, n ₅) b(n ₆ , b) P(n ₅ , n ₆)

$$\frac{P(n_0, n_1)}{n_0 = a, n_1 = b} \rightarrow q_9(a, b, n_0, n_1)$$

$$\frac{a(n_0, n_1)}{n_0 = a, n_1 \uparrow} \rightarrow q_1(a, b, n_0, n_1, b)$$

$$\frac{b(n_0, n_1)}{n_0 = a, n_1 \uparrow} \rightarrow q_2(a, b, n_0, n_1, b)$$

State $q_1(a, b, c, b)$

P(a, b)	→ a(a, c) . a(n ₁ , b) P(c, n ₁)
P(a, b)	→ a(a, c) . a(c, b)

$$\frac{a(n_0, n_1)}{n_0 = c, n_1 = b} \rightarrow q_3(a, b, n_0, n_1)$$

$$\frac{a(n_0, n_1)}{n_0 \uparrow, n_1 = b} \rightarrow q_4(a, b, n_0, n_1, c, n_0)$$

State $q_2(a, b, c, b)$

P(a, b)	→ b(a, c) . b(n ₁ , b) P(c, n ₁)
P(a, b)	→ b(a, c) . b(c, b)

$$\frac{b(n_0, n_1)}{n_0 = c, n_1 = b} \rightarrow q_5(a, b, n_0, n_1)$$

$$\frac{b(n_0, n_1)}{n_0 \uparrow, n_1 = b} \rightarrow q_6(a, b, n_0, n_1, c, n_0)$$

State $q_3(a, b, c)$

P(a, b)	→ a(a, c) a(c, b) . [aa]
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State $q_4(a, b, c, d)$

P(a, b)	→ a(a, c) a(d, b) . P(c, d)
P(c, d)	→ .a(c, n ₁) a(n ₁ , d)
P(c, d)	→ .a(c, n ₂) a(n ₃ , d) P(n ₂ , n ₃)
P(c, d)	→ .b(c, n ₄) b(n ₄ , d)
P(c, d)	→ .b(c, n ₅) b(n ₆ , d) P(n ₅ , n ₆)

$$\frac{P(n_0, n_1)}{n_0 = c, n_1 = d} \rightarrow q_7(a, b, n_0, n_1)$$

$$\frac{a(n_0, n_1)}{n_0 = c, n_1 \uparrow} \rightarrow q_1(n_0, d, n_1, d)$$

$$\frac{b(n_0, n_1)}{n_0 = c, n_1 \uparrow} \rightarrow q_2(n_0, d, n_1, d)$$

State $q_5(a, b, c)$

P(a, b)	→ b(a, c) b(c, b) . [bb]
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State $q_6(a, b, c, d)$

P(a, b)	→ b(a, c) b(d, b) . P(c, d)
P(c, d)	→ .a(c, n ₁) a(n ₁ , d)
P(c, d)	→ .a(c, n ₂) a(n ₃ , d) P(n ₂ , n ₃)
P(c, d)	→ .b(c, n ₄) b(n ₄ , d)
P(c, d)	→ .b(c, n ₅) b(n ₆ , d) P(n ₅ , n ₆)

$$\frac{P(n_0, n_1)}{n_0 = c, n_1 = d} \rightarrow q_8(a, b, n_0, n_1)$$

$$\frac{a(n_0, n_1)}{n_0 = c, n_1 \uparrow} \rightarrow q_1(n_0, d, n_1, d)$$

$$\frac{b(n_0, n_1)}{n_0 = c, n_1 \uparrow} \rightarrow q_2(n_0, d, n_1, d)$$

State $q_7(a, b, c, d)$

P(a, b)	→ a(a, c) a(d, b) P(c, d) . [aPa]
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State $q_8(a, b, c, d)$

P(a, b)	→ b(a, c) b(d, b) P(c, d) . [bPb]
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State $q_9(a, b)$

S()	→ P(a, b) . [init]
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